

1. Simplify each of the following

a) 6^{-2} c) $64^{-2/3}$ e) $8^{\log_2 5}$ g) $\log_3 4 \cdot \log_4 5 \cdot \log_5 6 - 1$ i) $e^{-2 \ln A}$
 b) $32^{3/5}$ d) $\log_9 \sqrt{27}$ f) $3^{\log_9 10}$ h) $\log_2 (4x^2) - 3 \log_2 \left(\frac{6}{x}\right) + \log_4 (4x^6)$

2. Let $x = \log_3 2$. Express each of the following in terms of x .

a) $\log_3 72$ b) $\log_2 3$ c) $\log_6 72$

3. Factor $3x^2 - 4x - 319$ by completing the square.

4. In case of each polynomial given, determine (by completing the square) whether it can be factored over the real numbers or not. (You do not have to actually factor.)

a) $20x + 2x^2 + 44$ b) $20x - 5x^2 - 25$

5. Solve the equation $9x^2 - 12x = 11$ and check one of your solution using exact values.

6. Solve each of the following equations. Present all solutions, in radians.

a) $\sin x + \sin 2x = 0$ b) $\sin x + \cos 2x = 0$ c) $\tan^3 x = 3 \tan x$

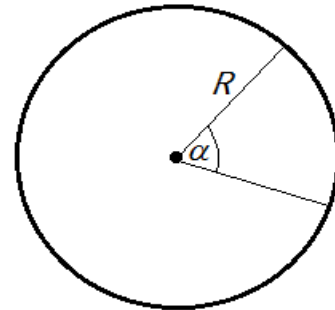
7. Suppose that α is a central angle (less than 360°) in a circle with radius R .

a) Express the length of the arc subtended by the central angle α in terms of α and R . Assume that α is measured in degrees.

b) Express the area of the sector determined by the central angle α in terms of α and R . Assume that α is measured in degrees.

c) Express the length of the arc subtended by the central angle α in terms of α and R . Assume that α is measured in radians.

d) Express the area of the sector determined by the central angle α in terms of α and R . Assume that α is measured in radians.



8. Solve each of the following equations.

a) $2x^3 = 6x$ d) $\log_3 (7 - x) + \log_3 (1 - x) = 3$
 b) $2x^2 - 3x - 1 = 0$ e) $\log_6 (-8 - x) + \log_6 (8 - x) = 2$
 c) $\log_2 (x + 5) - \log_2 (x - 7) = -1$ f) $\frac{2x - 1}{3} - \frac{x - 1}{2} = x - 4$

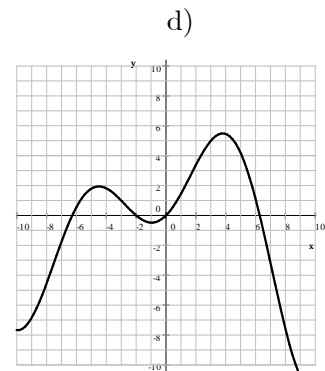
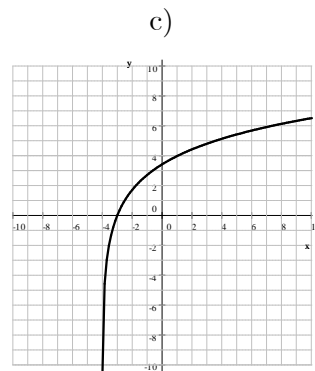
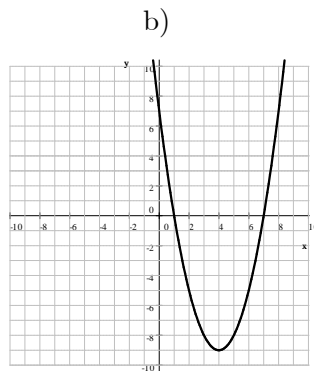
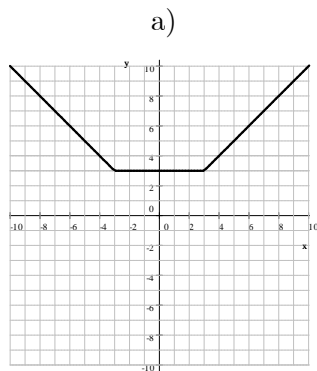
9. Solve each of the following inequalities.

a) $x^2 \geq 4x$ b) $8x + x^2 < 33$ c) $x^2 < -2x + 2$ d) $4x^2 \leq 4x - 1$ e) $x^2 - 6x > -10$

10. Find the domain for each of the following functions.

a) $f(x) = \ln(x^2 - 10x + 29)$ c) $f(x) = \log_5(x^2 - 10x + 21)$
 b) $g(x) = \frac{1}{\log_2(4 - x)}$ d) $k(x) = \frac{1}{\log_5(x^2 - 10x + 21)}$

11. a) Find the center and radius of a circle with equation $2y - 6x + x^2 + y^2 = 10$
 b) Find an equation for the tangent line drawn to the circle $(x + 2)^2 + (y - 4)^2 = 10$ to the point $(-5, 3)$
12. Find an equation for the curve that consists of points $P(x, y)$ with the following property: they are twice as far from point $A(2, -5)$ as from point $B(-1, 1)$. Describe the curve.
13. a) Solve the formula $V = 2\pi r^3 + \frac{1}{2}\pi r^2 h$ for h .
 b) A right pyramid has a square base with sides 30 meters long. The pyramid is 24 meters tall. At what height is the perpendicular cross section a square with sides 10 meters?
14. Graph each of the following pairs of functions in the same coordinate system.
 a) $f(x) = 2^x$ and $g(x) = \log_2 x$ b) $f(x) = 2^x$ and $g(x) = \left(\frac{1}{2}\right)^x$
 c) $f(x) = \log_2 x$ and $g(x) = \log_{1/2} x$ d) $f(x) = \left(\frac{1}{2}\right)^x$ and $g(x) = \log_{1/2} x$
15. For each of the following functions given, give a complete analysis and sketch its graph.
 a) $f(x) = 9 - 3x^2 - 6x$ on $[-2, 3]$ c) $f(x) = \log_3 x$ e) $f(x) = 1 + \sqrt{16 - x^2}$
 b) $f(x) = \sqrt{x + 3}$ d) $f(x) = 0.7^x$
16. Find the equation for the inverse for each of the following functions given.
 a) $f(x) = 3x - 1$ c) $h(x) = 1 + 3e^{2x-7}$ e) $m(x) = \frac{x-1}{2x+7}$
 b) $g(x) = \log_2(5x - 1)$ d) $p(x) = (x - 2)^3$
17. In each case, the graph of a function is given. Sketch the graph of the inverse relation in the same coordinate system.



18. An object's height (measured in feet) is defined by $s(t) = 0.4t + 12$ where t is the time, measured in seconds.
 a) Find the location of the object at $t = 10$ seconds.
 b) Find the average velocity of the object between $t = 0$ and $t = 3$ seconds
 c) Find the average velocity of the object between $t = 5$ and $t = 10$ seconds
19. An object's height (measured in feet) is defined by $s(t) = t^3 - 12t$ where t is the time, measured in seconds.
 a) Find the location of the object at $t = 3$ seconds.
 b) Find the average velocity of the object between
 i) $t = 0$ and $t = 2$ seconds ii) $t = 1$ s and $t = 2$ s iii) $t = 1.5$ s and $t = 2$

20. A bus travels between cities A and B. The distance between these cities is 60 miles. It takes the bus 2 hours to get from A to B. On its way back, the traveling time was only 1.5 hours. Find the average speed of the bus for
- a) the trip from A to B b) the trip from B to A c) for the roundtrip.
- d*) A bus travels between cities A and B. From A to B, the bus has an average speed of v_1 . On its way back, the average speed is v_2 . Express the average speed of the bus in terms of v_1 and v_2 .
21. Find the coordinates of all points where the graphs of $f(x) = x^2 - 2x - 26$ and $g(x) = 2x - 5$ intersect each other.
22. Compute each of the following limits.

a) $\lim_{x \rightarrow -\infty} (-2x^5 + 8x^2)$

i) $\lim_{x \rightarrow \infty} \frac{-x^3 + 2x + 1}{x - 3}$

p) $\lim_{x \rightarrow \infty} \frac{\sqrt{4 - \frac{1}{x}} - 2}{\frac{1}{x}}$

b) $\lim_{x \rightarrow \infty} (-2x^5 + 8x^2)$

j) $\lim_{x \rightarrow -\infty} 2^x$

c) $\lim_{x \rightarrow -\infty} (-2x^5 + 8x^6)$

k) $\lim_{x \rightarrow \infty} (\log_2(x^2 - 5x + 17))$

q) $\lim_{x \rightarrow -\infty} \frac{\cos x - 2}{x^3 + 1}$

d) $\lim_{x \rightarrow \infty} (-2x^5 + 8x^6)$

l) $\lim_{x \rightarrow \infty} \frac{12 + \log_7 3x}{15 + \log_7 x}$

r) $\lim_{x \rightarrow \infty} \tan x$

e) $\lim_{x \rightarrow -\infty} \frac{3x^2 - 1}{5x^2 - 3x + 2}$

m) $\lim_{x \rightarrow \infty} \frac{2^{x+5}}{4^{x-1}}$

s) $\lim_{x \rightarrow \infty} \frac{\ln 2x}{\ln 3x}$

f) $\lim_{x \rightarrow -\infty} \frac{100x - 1}{5x^2 - 3x + 2}$

n) $\lim_{x \rightarrow \infty} \frac{3^{x+1} \cdot \left(\frac{1}{3}\right)^{-x+2}}{9^{x-1}}$

t) $\lim_{\theta \rightarrow \infty} (\sin^2 \theta + \cos^2 \theta)$

g) $\lim_{x \rightarrow -\infty} \log_2 x$

o) $\lim_{x \rightarrow \infty} x \left(\frac{1}{3} - \frac{1}{3 - \frac{1}{x}} \right)$

u) $\lim_{x \rightarrow \infty} \frac{\sqrt{2x^2 - 1}}{x}$

23. Based on the graph of a function f shown on the picture, determine each of the following limits.

a) $\lim_{x \rightarrow 1^-} f(x)$

d) $\lim_{x \rightarrow 2^-} f(x)$

g) $\lim_{x \rightarrow 4^-} f(x)$

j) $\lim_{x \rightarrow 6^-} f(x)$

m) $\lim_{x \rightarrow 10^-} f(x)$

b) $\lim_{x \rightarrow 1^+} f(x)$

e) $\lim_{x \rightarrow 2^+} f(x)$

h) $\lim_{x \rightarrow 4^+} f(x)$

k) $\lim_{x \rightarrow 6^+} f(x)$

n) $\lim_{x \rightarrow 10^+} f(x)$

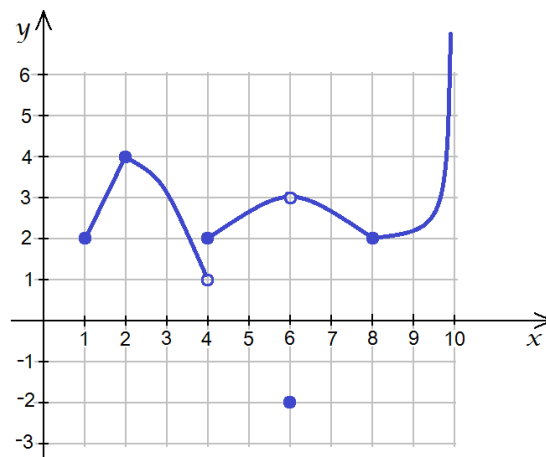
c) $\lim_{x \rightarrow 1} f(x)$

f) $\lim_{x \rightarrow 2} f(x)$

i) $\lim_{x \rightarrow 4} f(x)$

l) $\lim_{x \rightarrow 6} f(x)$

o) $\lim_{x \rightarrow 10} f(x)$



24. Compute each of the following limits.

a) $\lim_{x \rightarrow -\infty} \frac{x^2 - 9}{2x^2 - 8x + 6}$

e) $\lim_{x \rightarrow 1^-} \frac{x^2 - 9}{2x^2 - 8x + 6}$

i) $\lim_{x \rightarrow 3^+} \frac{x^2 - 9}{2x^2 - 8x + 6}$

b) $\lim_{x \rightarrow -3^-} \frac{x^2 - 9}{2x^2 - 8x + 6}$

f) $\lim_{x \rightarrow 1^+} \frac{x^2 - 9}{2x^2 - 8x + 6}$

j) $\lim_{x \rightarrow 3} \frac{x^2 - 9}{2x^2 - 8x + 6}$

c) $\lim_{x \rightarrow -3^+} \frac{x^2 - 9}{2x^2 - 8x + 6}$

g) $\lim_{x \rightarrow 1} \frac{x^2 - 9}{2x^2 - 8x + 6}$

k) $\lim_{x \rightarrow \infty} \frac{x^2 - 9}{2x^2 - 8x + 6}$

d) $\lim_{x \rightarrow -3} \frac{x^2 - 9}{2x^2 - 8x + 6}$

h) $\lim_{x \rightarrow 3^+} \frac{x^2 - 9}{2x^2 - 8x + 6}$

25. Based on your results in the previous problem, sketch the graph of $f(x) = \frac{x^2 - 9}{2x^2 - 8x + 6}$. (Plot a few additional points if needed.)

26. Compute each of the following limits.

a) $\lim_{x \rightarrow 2} \frac{2 - x}{\frac{1}{2} - \frac{1}{x}}$

f) $\lim_{x \rightarrow 1^+} \frac{x^2 - 9}{2x^2 - 8x + 6}$

l) $\lim_{a \rightarrow 0} \frac{\sqrt{5a + 4} - 2}{a}$

b) $\lim_{x \rightarrow 1^-} \frac{x^2 - 1}{2 - \sqrt{3 + x}}$

g) $\lim_{x \rightarrow 0} \frac{\sqrt{5 + x} - \sqrt{5}}{x}$

m) $\lim_{m \rightarrow 1^-} \frac{m^2 - 1}{m^4 - 1}$

c) $\lim_{x \rightarrow 3} \frac{|2x - 4|}{x - 8}$

h) $\lim_{x \rightarrow 3^-} \frac{x^2 - 9}{2x^2 - 8x + 6}$

n) $\lim_{x \rightarrow 0} \frac{1 + x + \sin x}{\cos x}$

d) $\lim_{x \rightarrow 0^-} \frac{|x|}{x}$

i) $\lim_{x \rightarrow \pi} \frac{\cos x}{\sin x}$

o) $\lim_{x \rightarrow \pi/3} (\tan^2 x - 1)$

e) $\lim_{x \rightarrow 0} \frac{|x|}{x}$

j) $\lim_{x \rightarrow \pi^+} \frac{\cos x}{\sin x}$

p) $\lim_{h \rightarrow 0} \frac{\sqrt{h^2 + 100} - 10}{h^2}$

k) $\lim_{x \rightarrow \pi/4} \tan x$

q) $\lim_{x \rightarrow 0^+} \ln x$

27. Consider the limit $\lim_{x \rightarrow \pi/2} \frac{1 - \tan^2 x}{1 + \tan^2 x}$.

a) Explain why we can not evaluate the limit in its current form.

b) Prove that $\frac{1 - \tan^2 x}{1 + \tan^2 x} = \cos 2x$ and use this to evaluate the limit.

28. Compute the derivative of each of the functions given by evaluating the limit of the difference quotient.

a) $f(x) = \sqrt{1 - 2x}$

b) $g(x) = \frac{1}{2 - x}$

c) $m(x) = 3x^2 - 5x$

29. Prove that if f and g are differentiable functions, then $(f + g)' = f' + g'$

30*. Consider the function $f(x) = 2mx - 8m + mx^2 + 3$ where m is a fixed real number.

a) Find all values of m for which the graph of f is NOT a parabola.

b) Graph $y = f(x)$ in the same coordinate system when $m = 0, 1$, and -1 .

c) Prove that there exist two points P and Q that are on the graph of $f(x)$ for all values of m .

Answers

1. a) $\frac{1}{36}$ b) 8 c) $\frac{1}{16}$ d) $\frac{3}{4}$ e) 125 f) $\sqrt{10}$ g) $\log_3 2 = \frac{\ln 2}{\ln 3}$ h) $\log_2 \left(\frac{x^8}{27} \right)$ i) $\frac{1}{A^2}$

2. a) $3x + 2$ b) $\frac{1}{x}$ c) $\frac{3x + 2}{x + 1}$

3. $3 \left(x + \frac{29}{3} \right) (x - 11) = (3x + 29) (x - 11)$

4. a) factors b) can not be factored

5. $\frac{2 \pm \sqrt{15}}{3}$ Check: if $x = \frac{2 - \sqrt{15}}{3}$, then the left-hand side of the equation is

$$\begin{aligned} \text{LHS} &= 9x^2 - 12x = 9 \left(\frac{2 - \sqrt{15}}{3} \right)^2 - 12 \left(\frac{2 - \sqrt{15}}{3} \right) = 9 \cdot \frac{(2 - \sqrt{15})^2}{9} - 12 \cdot \frac{2 - \sqrt{15}}{3} \\ &= (2 - \sqrt{15})^2 - 4(2 - \sqrt{15}) = 4 + 15 - 4\sqrt{15} - 8 + 4\sqrt{15} = 19 - 8 = 11 = \text{RHS} \end{aligned}$$

6. a) $x = k\pi$ or $x = \pm \frac{2\pi}{3} + 2k\pi$ where $k \in \mathbb{Z}$

b) $x = \frac{\pi}{2} + 2k\pi$ or $x = -\frac{\pi}{6} + 2k\pi$ or $x = -\frac{5\pi}{6} + 2k\pi$ where $k \in \mathbb{Z}$ c) $x = k\pi$ or $x = \pm \frac{\pi}{3} + k\pi$ where $k \in \mathbb{Z}$

7. a) $s = \frac{2\pi R\alpha}{360^\circ}$ b) $A = \frac{\pi R^2\alpha}{360^\circ}$ c) $s = R\alpha$ d) $A = \frac{1}{2}R^2\alpha$

8. a) $0, -\sqrt{3}, \sqrt{3}$ b) $\frac{3 \pm \sqrt{17}}{4}$ c) no solution d) -2 e) -10 f) 5

9. a) $(-\infty, 0] \cup [4, \infty)$ b) $(-11, 3)$ c) $(-\sqrt{3} - 1, \sqrt{3} - 1)$ d) $x = \frac{1}{2}$ e) \mathbb{R}

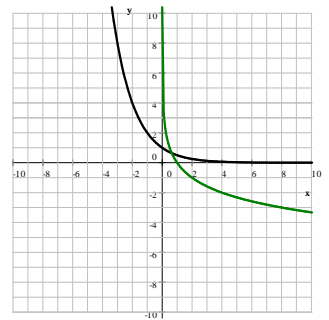
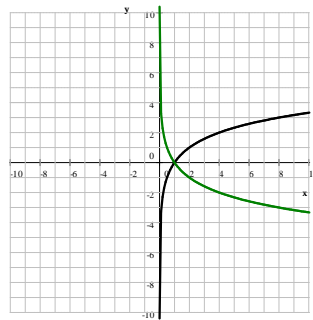
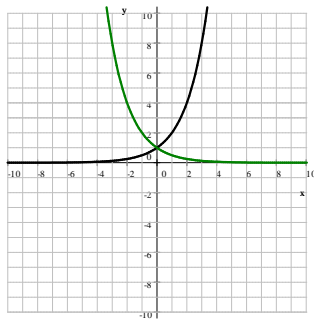
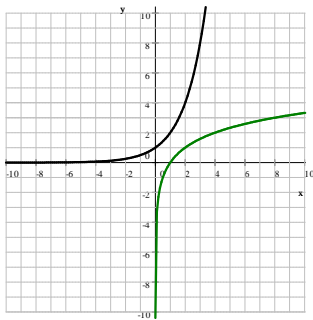
10. a) \mathbb{R} b) $x < 4$ but $x \neq 3$ c) $x < 3$ or $x > 7$
d) $x < 3$ but $x \neq 5 - \sqrt{5}$ or $x > 7$ but $x \neq 5 + \sqrt{5}$

11. a) center: $(3, -1)$ radius: $2\sqrt{5}$ b) $y = -3x - 12$

12. $(x + 2)^2 + (y - 3)^2 = 20$ a circle, centered at $(-2, 3)$ with radius $\sqrt{20}$

13. a) $h = \frac{2(V - 2\pi r^3)}{\pi r^2}$ or $h = \frac{2V}{\pi r^2} - 4r$ b) At a height of 16 meters

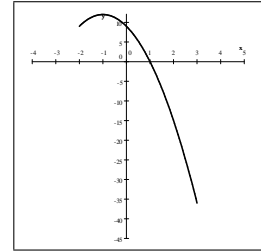
14. a) b) c) d)



15. a) $f(x) = 9 - 3x^2 - 6x$ on $[-2, 3]$

domain: $[-2, 3]$
 range: $[-36, 12]$
 x -intercept: $(1, 0)$
 y -intercept: $(0, 9)$
 maximum: $(-1, 12)$
 minimum: $(3, -36)$

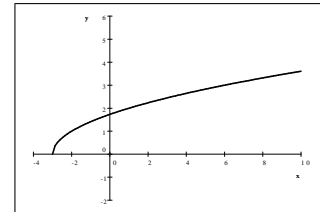
and decreasing on $(-1, 3)$
 one-to-one: no
 end-behavior: none
 i.e. $\lim_{x \rightarrow \pm\infty} f(x) = \text{undefined}$



b) $f(x) = \sqrt{x+3}$

domain: $[-3, \infty)$
 range: $[-3, \infty)$
 x -intercept: $(-3, 0)$
 y -intercept: $(0, \sqrt{3})$
 maximum: none
 minimum: $(-3, 0)$

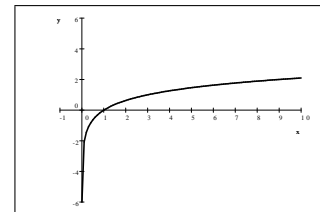
one-to-one: yes
 end-behavior:
 $\lim_{x \rightarrow -\infty} f(x) = \text{undefined}$
 and $\lim_{x \rightarrow \infty} f(x) = \infty$



c) $f(x) = \log_3 x$

domain: $(0, \infty)$
 range: \mathbb{R}
 x -intercept: $(1, 0)$
 y -intercept: none
 maximum: none
 minimum: none

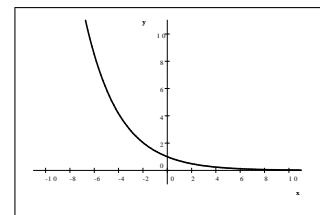
one-to-one: yes
 end-behavior:
 $\lim_{x \rightarrow -\infty} f(x) = \text{undefined}$
 and $\lim_{x \rightarrow \infty} f(x) = \infty$



d) $f(x) = 0.7^x$

domain: \mathbb{R}
 range: $(0, \infty)$
 x -intercept: none
 y -intercept: $(0, 1)$
 maximum: none
 minimum: none

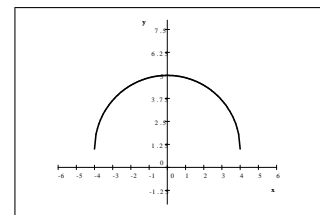
one-to-one: yes
 end-behavior:
 $\lim_{x \rightarrow -\infty} f(x) = \infty$
 and $\lim_{x \rightarrow \infty} f(x) = 0$



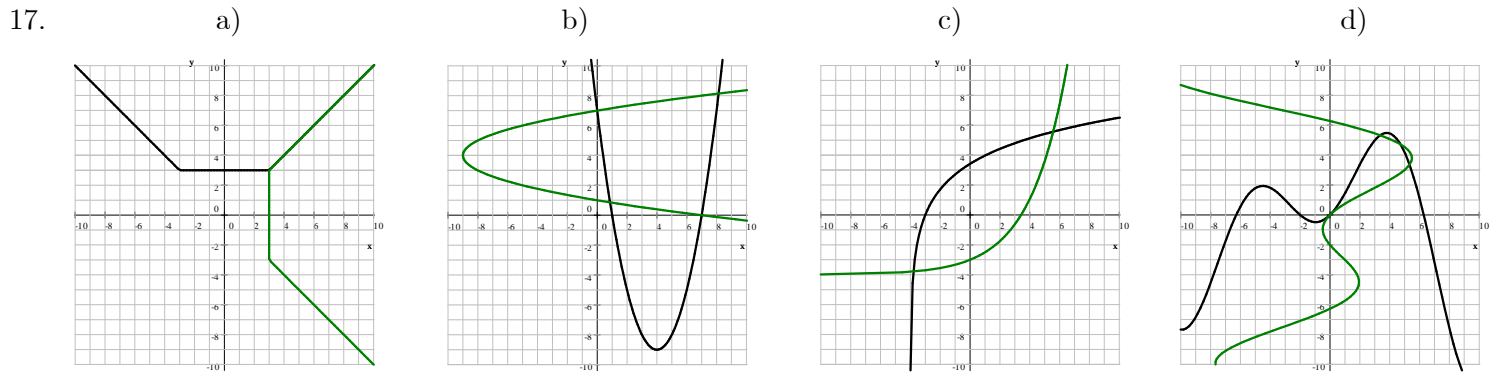
e) $f(x) = 1 + \sqrt{16 - x^2}$

domain: $[-4, 4]$
 range: $[1, 5]$
 x -intercept: none
 y -intercept: $(0, 5)$
 maximum: $(0, 5)$
 minimum: $(-4, 1)$ and $(4, 1)$

one-to-one: no
 end-behavior:
 $\lim_{x \rightarrow -\infty} f(x) = \text{undefined}$
 and $\lim_{x \rightarrow \infty} f(x) = \text{undefined}$



16. a) $f^{-1}(x) = \frac{1}{3}x + \frac{1}{3}$ b) $g^{-1}(x) = \frac{1}{5}(2^x + 1)$ c) $h^{-1}(x) = \frac{1}{2} \ln\left(\frac{x-1}{3}\right) + \frac{7}{2}$ d) $p^{-1}(x) = \sqrt[3]{x} + 2$
 e) $m^{-1}(x) = \frac{7x+1}{-2x+1}$



18. a) 16 ft b) $0.4 \frac{\text{ft}}{\text{s}}$ c) $0.4 \frac{\text{ft}}{\text{s}}$

19. a) -9 ft b) i) $-8 \frac{\text{ft}}{\text{s}}$ ii) $-5 \frac{\text{ft}}{\text{s}}$ iii) $-2.75 \frac{\text{ft}}{\text{s}}$

20. a) $30 \frac{\text{mi}}{\text{h}}$ b) $40 \frac{\text{mi}}{\text{h}}$ c) $\frac{240 \text{ mi}}{7 \text{ h}} \approx 34.2857143 \frac{\text{mi}}{\text{h}}$ d) $\frac{2v_1v_2}{v_1 + v_2}$

21. (7, 9) and (-3, -11)

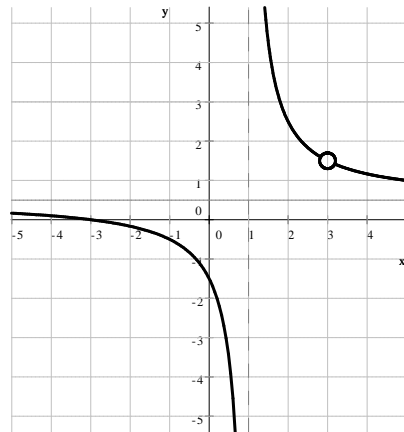
22. a) ∞ b) $-\infty$ c) ∞ d) ∞ e) $\frac{3}{5}$ f) 0 g) undefined h) $\frac{2}{3}$ i) $-\infty$ j) 0
 k) ∞ l) 1 m) 0 n) 3 o) $-\frac{1}{9}$ p) $-\frac{1}{4}$ q) 0 r) undefined s) 1 t) 1 u) $\sqrt{2}$

23. a) undefined b) 2 c) undefined d) 4 e) 4 f) 4 g) 1 h) 2 i) undefined
 j) 3 k) 3 l) 3 m) ∞ n) undefined o) undefined

24. a) $\frac{1}{2}$ b) 0 c) 0 d) 0 e) $-\infty$ f) ∞
 g) undefined h) $\frac{3}{2}$ i) $\frac{3}{2}$ j) $\frac{3}{2}$ k) $\frac{1}{2}$

25. see picture on the right

26. a) -4 b) -8 c) $-\frac{2}{5}$ d) -1
 e) undefined f) ∞ g) $\frac{\sqrt{5}}{10}$ h) $\frac{3}{2}$
 i) undefined j) ∞ k) 1 l) $\frac{5}{4}$ m) $\frac{1}{2}$
 n) 1 o) 2 p) $\frac{1}{20}$ q) $-\infty$



27. a) $\tan \frac{\pi}{2}$ is undefined and the tangent function approaches infinity (and negative infinity) as x approaches $\frac{\pi}{2}$. In short, $\lim_{x \rightarrow \pi/2^-} \tan x = \infty$ and $\lim_{x \rightarrow \pi/2^+} \tan x = -\infty$. So the limit as stated is a $\frac{-\infty}{\infty}$ type of an indeterminate.

b) $\frac{1 - \tan^2 x}{1 + \tan^2 x} = \frac{1 - \frac{\sin^2 x}{\cos^2 x}}{1 + \frac{\sin^2 x}{\cos^2 x}}$ we multiply numerator and denominator by $\cos^2 x$.

$$\frac{1 - \frac{\sin^2 x}{\cos^2 x}}{1 + \frac{\sin^2 x}{\cos^2 x}} = \frac{1 - \frac{\sin^2 x}{\cos^2 x}}{1 + \frac{\sin^2 x}{\cos^2 x}} \cdot \frac{\cos^2 x}{\cos^2 x} = \frac{\cos^2 x - \sin^2 x}{\cos^2 x + \sin^2 x} = \frac{\cos 2x}{1} = \cos 2x$$

Thus the limit is $\lim_{x \rightarrow \pi/2} \frac{1 - \tan^2 x}{1 + \tan^2 x} = \lim_{x \rightarrow \pi/2} \cos 2x = \cos \pi = -1$

28.

$$\begin{aligned} f'(x) &= \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \rightarrow 0} \frac{\sqrt{1-2(x+h)} - \sqrt{1-2x}}{h} = \lim_{h \rightarrow 0} \frac{\sqrt{1-2(x+h)} - \sqrt{1-2x}}{h} \cdot 1 \\ &= \lim_{h \rightarrow 0} \frac{\sqrt{1-2(x+h)} - \sqrt{1-2x}}{h} \cdot \frac{\sqrt{1-2(x+h)} + \sqrt{1-2x}}{\sqrt{1-2(x+h)} + \sqrt{1-2x}} = \lim_{h \rightarrow 0} \frac{1-2x-2h-(1-2x)}{h(\sqrt{1-2(x+h)} + \sqrt{1-2x})} \\ &= \lim_{h \rightarrow 0} \frac{1-2x-2h-1+2x}{h(\sqrt{1-2(x+h)} + \sqrt{1-2x})} = \lim_{h \rightarrow 0} \frac{-2h}{h(\sqrt{1-2(x+h)} + \sqrt{1-2x})} \\ &= \lim_{h \rightarrow 0} \frac{-2}{\sqrt{1-2(x+h)} + \sqrt{1-2x}} = \frac{-2}{\sqrt{1-2x} + \sqrt{1-2x}} = \frac{-2}{2\sqrt{1-2x}} = \frac{-1}{\sqrt{1-2x}} \end{aligned}$$

$$\begin{aligned} g'(x) &= \lim_{h \rightarrow 0} \frac{g(x+h) - g(x)}{h} = \lim_{h \rightarrow 0} \frac{\frac{1}{2-(x+h)} - \frac{1}{2-x}}{h} = \lim_{h \rightarrow 0} \frac{\frac{1}{2-x-h} - \frac{1}{2-x}}{h} \\ &= \lim_{h \rightarrow 0} \frac{\frac{(2-x) - (2-x-h)}{(2-x-h)(2-x)}}{h} = \lim_{h \rightarrow 0} \frac{2-x-2+x+h}{h(2-x-h)(2-x)} \cdot \frac{1}{h} = \lim_{h \rightarrow 0} \frac{h}{h(2-x-h)(2-x)} \\ &= \lim_{h \rightarrow 0} \frac{1}{(2-x-h)(2-x)} = \frac{1}{(2-x)(2-x)} = \frac{1}{(2-x)^2} \end{aligned}$$

$$\begin{aligned} m'(x) &= \lim_{h \rightarrow 0} \frac{m(x+h) - m(x)}{h} = \lim_{h \rightarrow 0} \frac{[3(x+h)^2 - 5(x+h)] - [3x^2 - 5x]}{h} \\ &= \lim_{h \rightarrow 0} \frac{[3(x^2 + 2xh + h^2) - 5(x+h)] - [3x^2 - 5x]}{h} = \lim_{h \rightarrow 0} \frac{[3x^2 + 6xh + 3h^2 - 5x - 5h] - [3x^2 - 5x]}{h} \\ &= \lim_{h \rightarrow 0} \frac{3x^2 + 6xh + 3h^2 - 5x - 5h - 3x^2 + 5x}{h} = \lim_{h \rightarrow 0} \frac{6xh + 3h^2 - 5h}{h} = \lim_{h \rightarrow 0} \frac{h(6x + 3h - 5)}{h} \\ &= \lim_{h \rightarrow 0} (6x + 3h - 5) = 6x - 5 \end{aligned}$$

29. see handout titled Differentiation 1

30. a) 0 b) see below c) $y = m(x-2)(x+4) + 3$ No matter what m is, $(2, 3)$ and $(-4, 3)$ will be on the graph

